

Fire resistance of concrete slabs acting in compressive membrane action

No need for steel anymore?

11th of April 2017 – IStructE HQ London



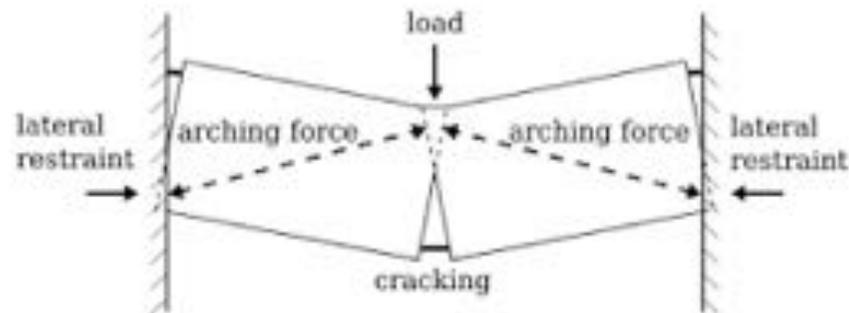
STRUCTURES IN FIRE FORUM

Introduction

- Bearing capacity of (existing) slabs?
- Experiences in building renovations with a surprising low capacity following classic bending theory, mostly with rather thin slabs.
- No excessive deformations noted before => no tensile membrane action involved but probably compressive membrane action.
- What about fire resistance of such slabs?

Compressive membrane action (CMA)

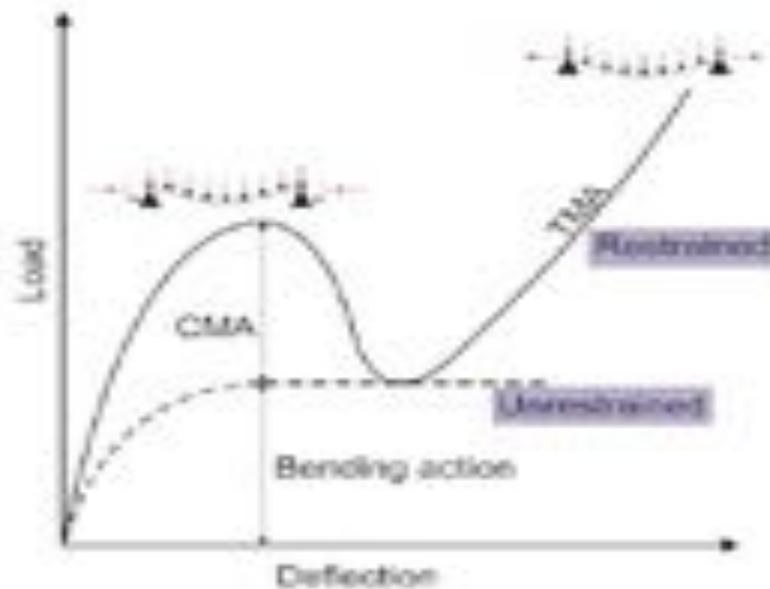
- The arch effect – compressive membrane action



- Lateral restraint capable to withstand compressive forces

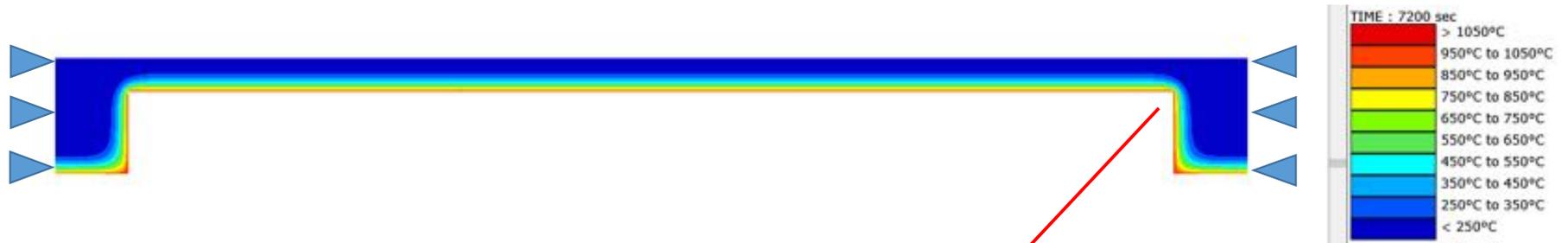
Compressive membrane action (CMA)

- CMA mechanism fails due to concrete crushing => TMA or failure

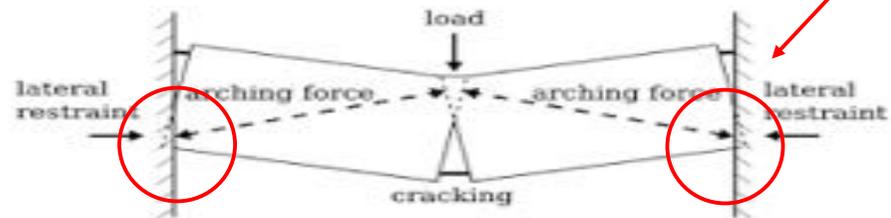


CMA at elevated temperature

- Isothermal lines



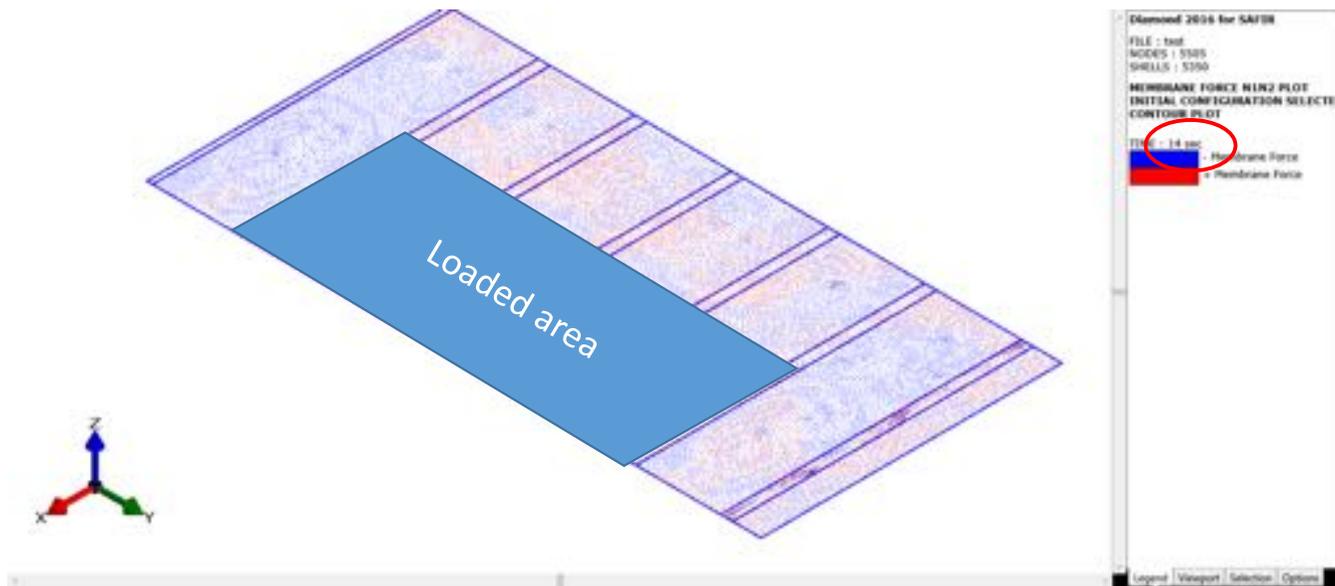
- Behaviour at the origin of arches?



CMA with FEM models?

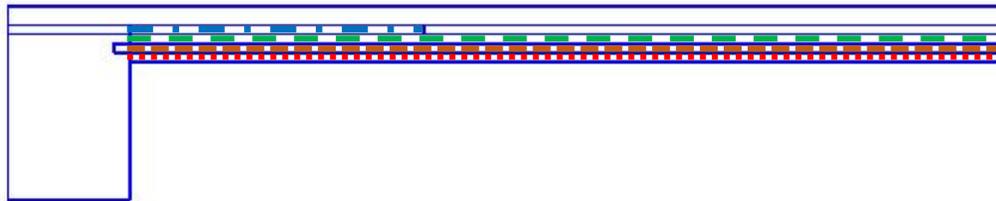
- By the aid of plane elements with bending and membrane behaviour.
- Advanced material model (Explicit Transient Creep).
- At ambient conditions, time dependent load function (20s)

- Stops at 70%
- Doesn't work



CMA with FEM models?

- Vertical section with superimposed layers of shell elements
- Advanced material model (Explicit Transient Creep).
- At ambient conditions, time dependent load function (20s)
- Rebar elements



- Adding elevated temperature profile pro layer is quiet simple

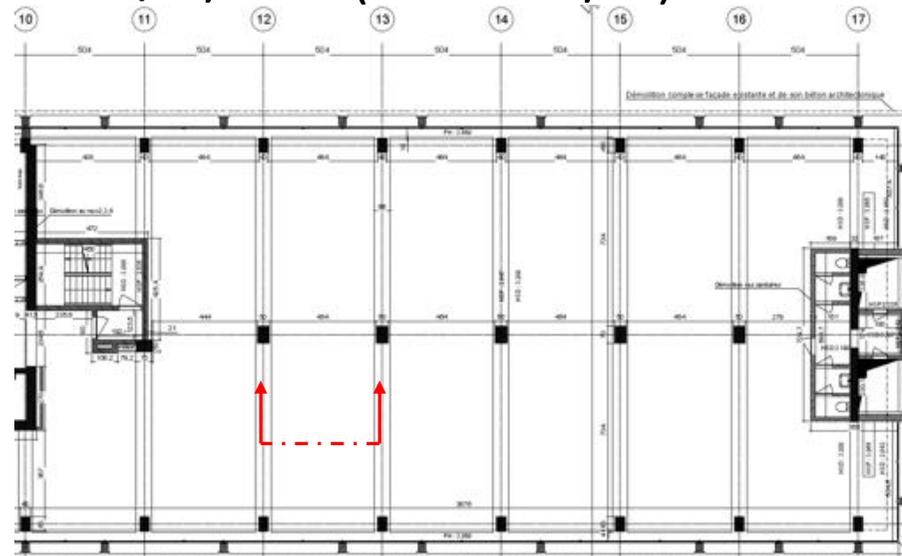
Case study – building description

- Leopold tower in Brussels near the NATO (Evere).
- Office building in the past with screed and mobile load of 3 kN/m²
- Slab of 0.14 m, 5.04 m span, width 16.5m, upper (curtailed) and lower principal reinforcement = Ø8/0.15 (335 mm²/m)



Half floor:

Section

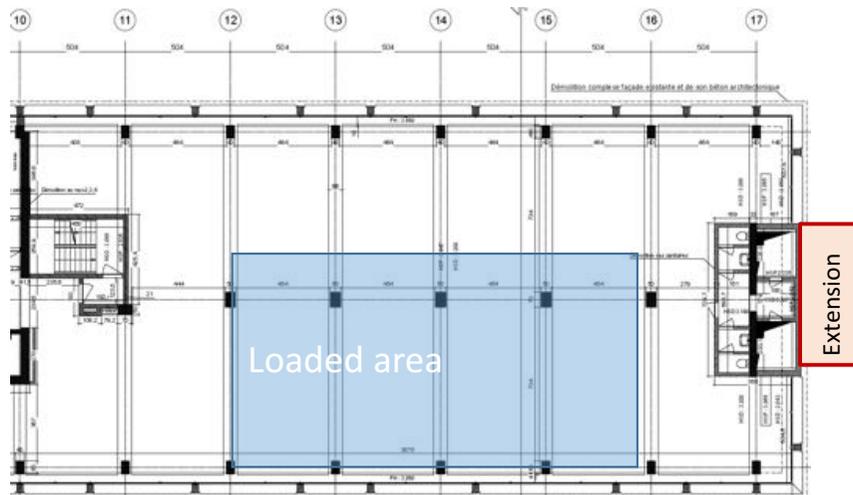


Case study – building description

- Transformation into an apartment building with reduced mobile loads but increased super imposed dead loads.
- Out of bending theory; insufficient reinforcement even for the existing situation.
- But restraints available at the extremes => CMA possible?
- Due to high costs of external reinforcement + fire protection and possible benefits the owner agreed with a load test.

Case study – Test set-up

- Load test done till ULS-values (for ambient conditions); 11.58 kN/m^2
- Swimming pools of 0.8 m + DL.



Case study – Bearing capacity

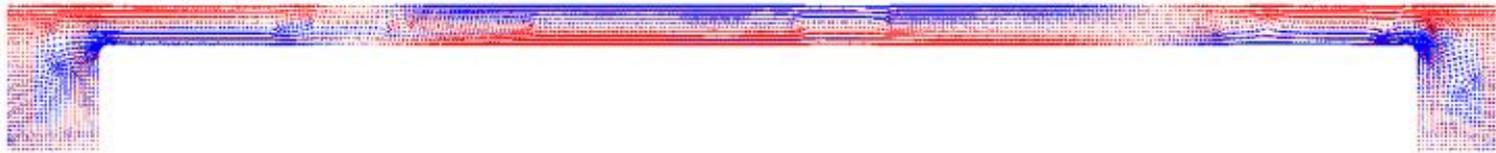
- Elastic bending theory

$$M_{Rd} = \left(h - c_{centre} - \frac{x}{2} \right) A_s f_{yd} = \left(h - c_{centre} - \frac{A_s f_{yd}}{2b f_{cd}} \right) A_s f_{yd}$$

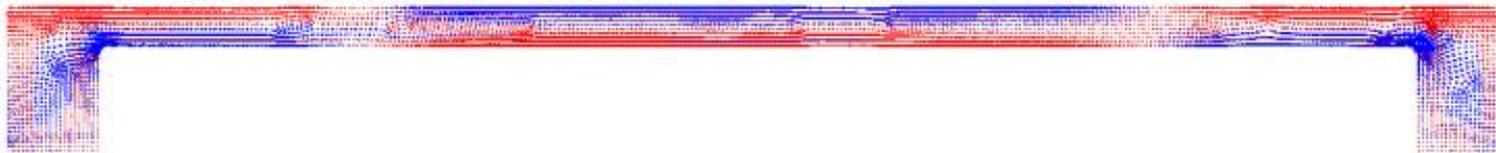
- Span 13.17 kNm, hogging moments 11.52 kNm with sum 24.69 kNm
- With $\Sigma M = wL^2/8 \Rightarrow w < 7.78 \text{ kN/m}^2$ and needed + test 11.58 kN/m^2 ?
- Only dead loads are representing already 6.18 kN/m^2 (factored)
- Plastic analysis with membrane action results in 0.35 m deformation!
- Measured deformations of only a few mm
- Only CMA can explain this behaviour

Case study – FEM @ ambient temperature

- CMA simulation without reinforcement
- Full load available after 20 s with equal increments/time step
- Principal stresses at 10.7 s (about DL) & 12.5 s



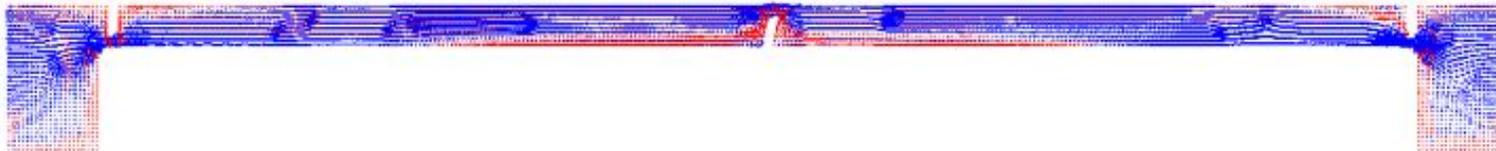
^ Diamond 2016 for SAFIR
FILE : sh1_amb
NODES : 1194
SHELLS : 1000
MEMBRANE FORCE N1N2 PLOT
INITIAL CONFIGURATION SELECTED
TIME : 10,9 sec
- Membrane Force
+ Membrane Force



^ Diamond 2016 for SAFIR
FILE : sh1_amb
NODES : 1194
SHELLS : 1000
MEMBRANE FORCE N1N2 PLOT
INITIAL CONFIGURATION SELECTED
TIME : 12,5 sec
- Membrane Force
+ Membrane Force

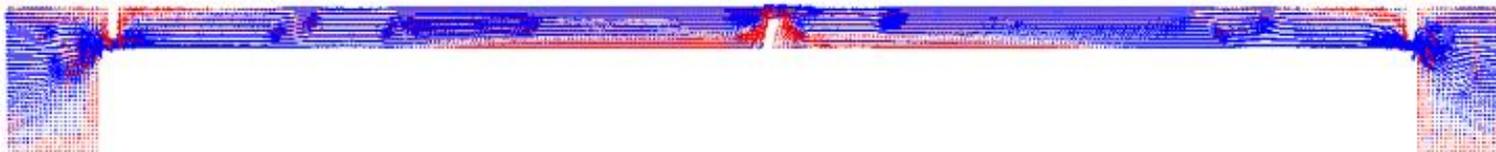
Case study – FEM @ ambient temperature

- Principal stresses at 13.5 s



Diamond 2016 for SAFIR
FILE : sh1_amb
NODES : 1194
SHELLS : 1000
**MEMBRANE FORCE N1N2 PLOT
INITIAL CONFIGURATION SELECTED**
TIME : 13,50686 sec
- Membrane Force
+ Membrane Force

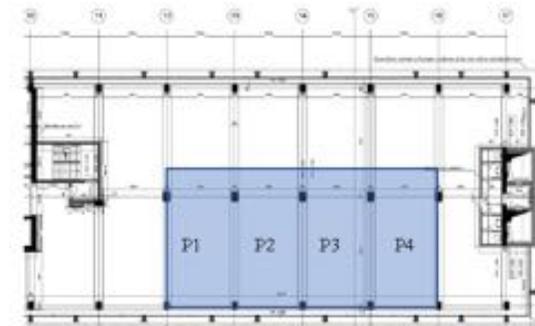
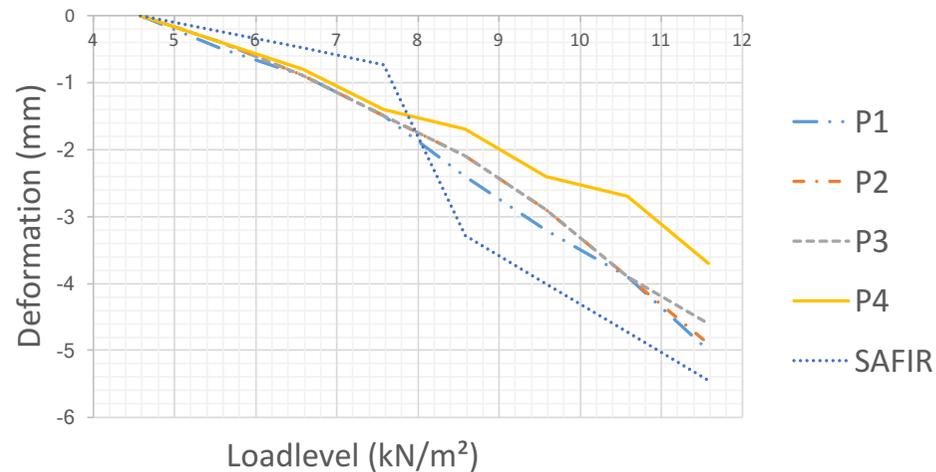
- Principal stresses at 20.0 s



Diamond 2016 for SAFIR
FILE : sh1_amb
NODES : 1194
SHELLS : 1000
**MEMBRANE FORCE N1N2 PLOT
INITIAL CONFIGURATION SELECTED**
TIME : 20 sec
- Membrane Force
+ Membrane Force

Case study – FEM @ ambient temperature

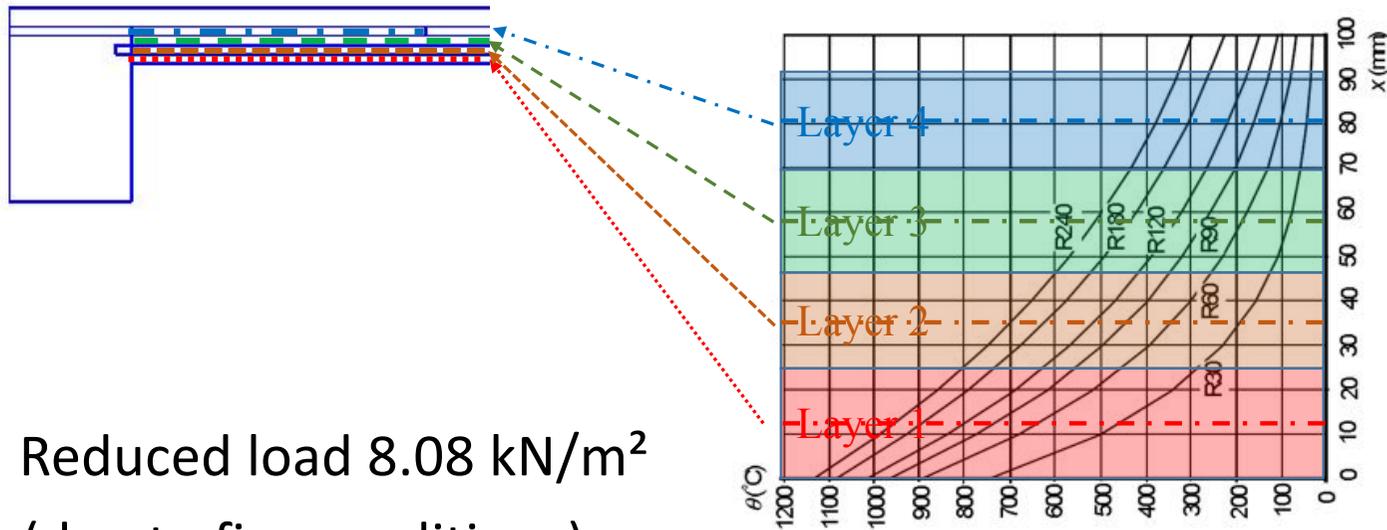
- Measured deformations related to computed values



- Seems to correspond on a reasonable way 😊

Case study – FEM @ elevated temperature

- Temperature profiles out of NBN EN 1992-1-2



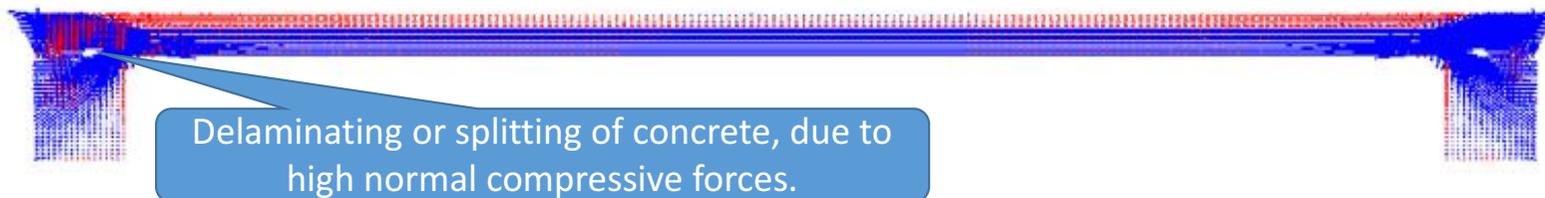
- Reduced load 8.08 kN/m^2
(due to fire conditions)

Case study – FEM @ elevated temperature

- Principal stresses at 20.0 s with layered shell elements

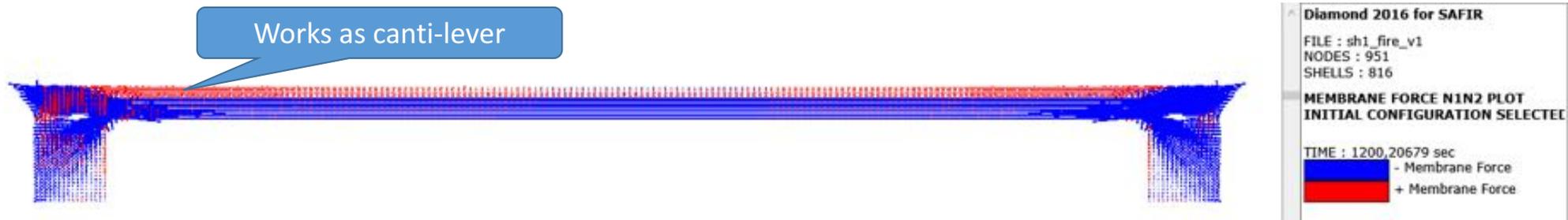


- Principal stresses at 900 s (delaminating starts)

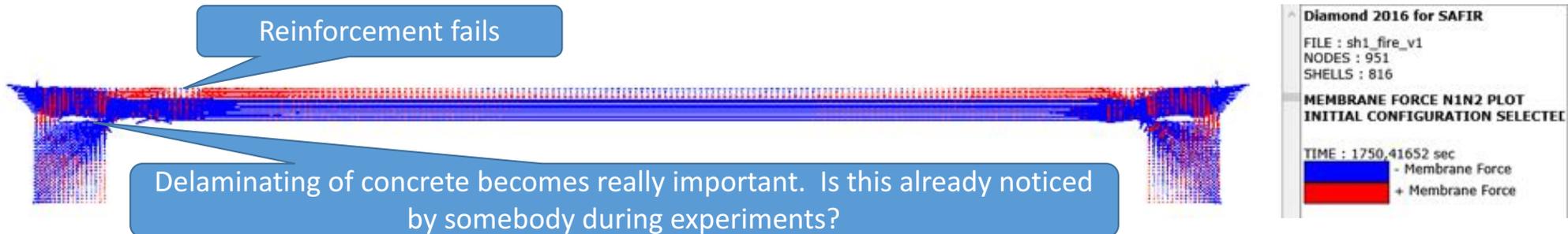


Case study – FEM @ elevated temperature

- Principal stresses at 1200 s

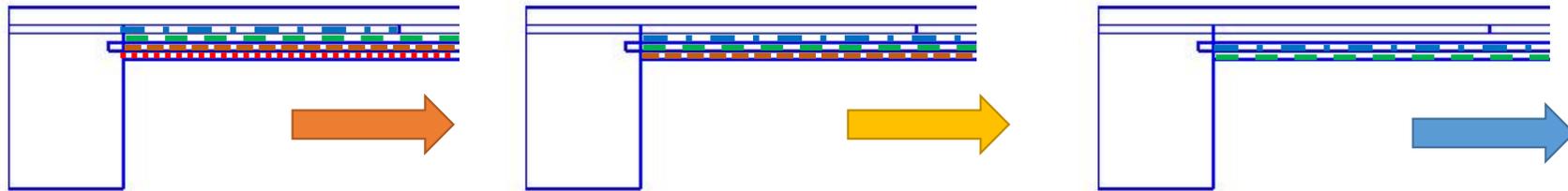


- Principal stresses at 1750 s (cracks on top and termination/failure)

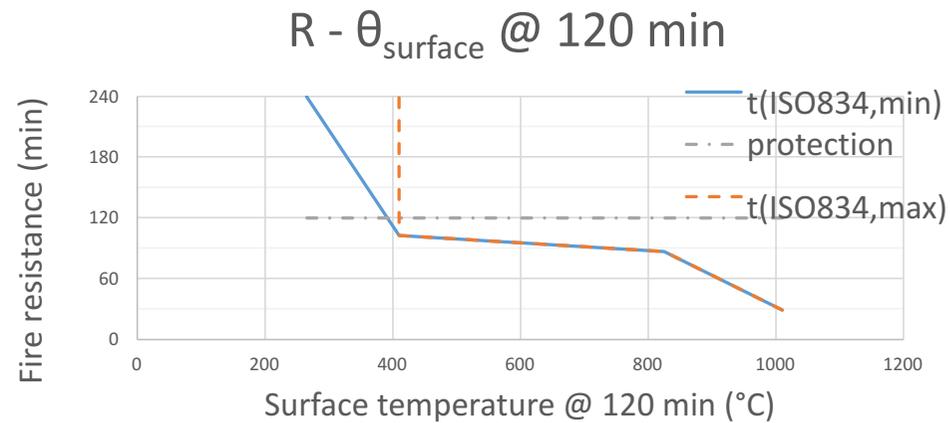


Case study – Failure time with protection

- Temperature profiles out of NBN EN 1992-1-2

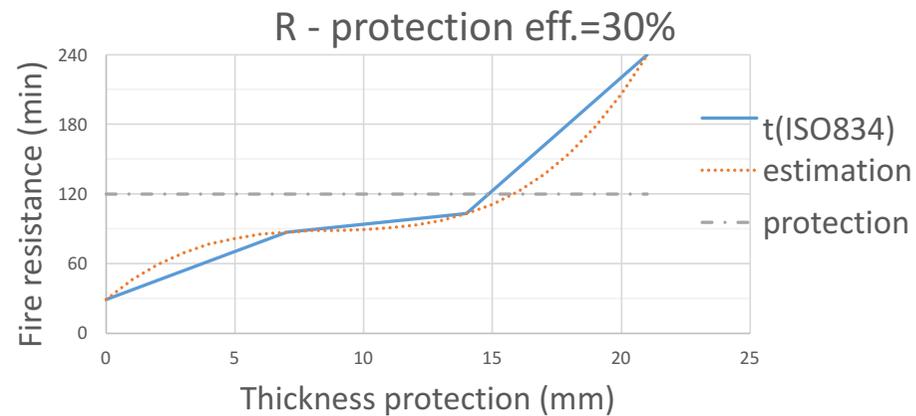


- Protection time



Case study – Failure time with protection

- Protection material; presume the same efficiency as one layer of 23 mm of concrete:



Simplifications – engineering judgement

•Let's try the simple way:

1. At ambient temperature, the horizontal reaction force is computed as: $H_{sd} = M_{sd}/z = p_{sd} \cdot L^2 / (8 \cdot z)$ with z = the lever arm or arch camber, p_{sd} = design load and L the span.
2. The depth of the compression area is: $x = H_{sd} / (b \cdot f_{cd})$ with b the slab width and f_{cd} the design concrete strength in compression.
3. The lever arm is modified to account for the depth x : $z = h - x/2$ with h the slab height; some iterations may be required from 1 to 3 to find the final value of the lever arm.

Simplifications – engineering judgement

• Let's try the simple way:

1. In case of fire, the applied load is lower than the design load at ambient temperature; hence the horizontal reaction force is reduced as: $H_{fi} = p_{fi} \cdot L^2 / (8 \cdot z_{fi})$ with z_{fi} = lever arm and p_{fi} = load in case of fire.
2. The depth of the compression area in case of fire is: $x_{fi} = H_{fi} / (b \cdot f_{\theta})$. Looking to *Fig. 1a*, the temperature θ of the lower part of the slab will be important at the origins of the arch.
3. The lever arm is modified to account for the depth x_{fi} : $z_{fi} = h - (x_{fi}/2)$; some iterations may be required from 1 to 3 to find the final value of the lever arm in case of fire.
4. Finally, the verification of structural safety in the fire situation is performed as: as long as $H_{fi} < H_{Sd}$, the slab is able to sustain the load in the fire situation.

Simplifications – engineering judgement

• Let's try the simple way:

1. In case of fire, the applied load is lower than the design load at ambient temperature; hence the horizontal reaction force is reduced as: $H_{fi} = p_{fi} \cdot L^2 / (8 \cdot z_{fi})$ with z_{fi} = lever arm and p_{fi} = load in case of fire.
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3. The lever arm is modified to account for the depth x_{fi} : $z_{fi} = h - (x_{fi} / 2)$; some iterations may be required from 1 to 3 to find the final value of the lever arm in case of fire.
4. Finally, the verification of structural safety in the fire situation is performed as: as long as $H_{fi} < H_{Sd}$, the slab is able to sustain the load in the fire situation.

Simplifications – engineering judgement

• Case study => doubtful result ?

1. $H_{Sd} = M_{Sd}/z = 11.58 \cdot 5.04^2 / (8 \cdot 0.133) = 276.46 \text{ kN/m}$ with $z = 0.95 \cdot 0.140 = 0.133$
2. $x = 276.46 / (0.85 \cdot 30 / 1.5) = 16.26 \text{ mm}$, hence take 16 mm.
3. $z = 0.140 - 0.016/2 = 0.132 \text{ m}$ which can be considered as converged, taking into account 1 % deviation compared with 0.133.
4. $H_{fi} = 8.08 \cdot 5.04^2 / (8 \cdot z_{fi}) \leq 276.46 \text{ kN/m}$ which leads to $z_{fi} \geq 0.093 \text{ m}$
5. $z_{fi} = 0.140 - (x_{fi}/2) \geq 0.093$ or $x_{fi} \leq 0.093 \text{ m}$
6. $x_{fi} = 276.46 / (f_{c\theta} / f_{ck} \cdot 30) \leq 93 \text{ mm}$, the maximum allowable reduction to respect this equilibrium is obtained if $f_{c\theta} / f_{ck} \geq 0.10$ and can be applied at the origin of the arch. Take this equal to the one corresponding to the temperature in the ultimate fiber of the layer as a rough and save simplification. Following table 3.1 of EC2-1-2 [4] this means 871 °C would be acceptable, which appears at $R57 < R120$ required but $> R29$ following SAFIR analysis

Further developments

- Punching problem:
 - Has the same failure behaviour
 - Is related to the same mechanism
 - But we even don't understand and agree about at ambient conditions.
- ...
- ...

Conclusions

- CMA can play a major role in restrained structures. With advanced FEM-analysis and suitable material models this can be simulated with a reasonable agreement for the vertical deformations.
- Modelling at elevated temperatures is even more challenging, however maximum surface temperatures could be derived for a practical case study and subsequently the needed fire protection.
- Our understanding of CMA is still too limited to build up simple engineering models.

Thanks for the kind attention



Sweco Belgium nv

Locaties: Antwerpen, Brugge,
Brussel, Gent, Hasselt, Herentals,
Mechelen, Wavre, Zelzate

Herkenrodesingel 8B, bus 3.01
B-3500 Hasselt
T +32 11 26 08 70
F +32 11 23 38 28
hasselt@swecobelgium.be
www.swecobelgium.be

Q&A ?

Tom Molkens
Thomas Gernay (ULg)
Robby Caspeele (UGent)

BTW BE 0405.647.664
RPR Brussel

BNP PARIBAS FORTIS IBAN:
BE97 2200 7208 2049 BIC:
GEBABEBB

Maatschappelijke zetel
Sweco Belgium nv
Arenbergstraat 13, bus 1
B-1000 Brussel

2nd International Fire
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Naples, 7-9 June
IFireSS 2017

